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# **Programmable Differential Bandgap Reference Circuit for Ultra-Low-Power CMOS LSIs**

**Yoshinori ITOTAGAWA**†a)**, Koma ATSUMI**† **, Hikaru SEBE**† **,** *Nonmembers***, Daisuke KANEMOTO**† **,** *and* **Tetsuya HIROSE**†b) **,** *Members*

**SUMMARY** This paper describes a programmable differential bandgap reference (PD-BGR) for ultra-low-power IoT (Internet-of-Things) edge node devices. The PD-BGR consists of a current generator (CG) and differential voltage generator (DVG). The CG is based on a bandgap reference (BGR) and generates an operating current and a voltage, while the DVG generates another voltage from the current. A differential voltage reference can be obtained by taking the voltage difference from the voltages. The PD-BGR can produce a programmable differential output voltage by changing the multipliers of MOSFETs in a differential pair and resistance with digital codes. Simulation results showed that the proposed PD-BGR can generate 25- to 200-mV reference voltages with a 25-mV step within a  $\pm$ 0.7% temperature inaccuracy in a temperature range from -20 to 100◦C. A Monte Carlo simulation showed that the coefficient of the variation in the reference was within 1.1%. Measurement results demonstrated that our prototype chips can generate stable programmable differential output voltages, almost the same results as those of the simulation. The average power consumption was only 88.4 nW, with a voltage error of −4/+3 mV with 5 samples.

*key words: Internet-of-Things (IoT), bandgap voltage reference, programmable reference, differential voltage reference*

# **1. Introduction**

Ultra-low-power analog, digital, and mixed-signal CMOS LSIs are strongly required to realize next-generation IoT (Internet-of-Things) edge node devices  $[1]$ [–\[6\].](#page-6-1) They will have the power to change the world we live in. Voltage references (VRs) are one of basic and important circuit building blocks for processing analog signal information and converting physical information into digital form. They are used in various circuits, such as analog-to-digital Converters (ADCs), digital-to-analog Converters (DACs), power management circuits (PMCs), low-dropout linear regulators (LDOs), and versatile sensor interface circuits. Therefore, we must develop ultra-low power and high precision VRs for such IoT edge node devices.

Various VRs capable of operating with nano-watt (nW) power, or less, have been investigated [\[7\]–](#page-6-2)[\[13\]](#page-6-3). The reference voltages of these VRs are based on the bandgap voltage of silicon  $(V_{\text{BGR}})$  [\[7\],](#page-6-2) [\[8\]](#page-6-4), threshold voltage  $(V_{\text{TH}})$ of a MOSFET [\[9\]](#page-6-5), [\[10\]](#page-6-6), and threshold voltage difference

b) E-mail: hirose@eei.eng.osaka-u.ac.jp

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 $(\Delta V_{TH})$  [\[11\]](#page-6-7)[–\[14\]](#page-6-8). However, almost all of them are realized in a single-ended configuration, so differential or programmable VRs have not been adequately considered. A differential and programmable VR could be useful and advantageous, especially when it must directly interface itself with other differential circuit blocks [\[15\]](#page-6-9)[–\[22\].](#page-6-10) This would lead to a superior noise-immunity and high process-stability for the overall system. In addition, such VRs can be utilized for generating functional and intelligent temperature sensor current [\[23\]–](#page-6-11)[\[25\]](#page-7-0). In the studies, two reference voltages that have a constant voltage difference are required to generate a sensor signal. However, these voltages are supplied from an off-chip voltage source. Thus, an on-chip differential VR is required. Some programmable differential VRs have been reported [\[19\],](#page-6-12) [\[20\].](#page-6-13) However, the generated output voltages are higher than 1 V and power consumption is in the order of several tens of microwatts. Thus, they have difficulties in low-voltage and low-power operation.

In light of this background, we present a low-voltage programmable differential bandgap reference (PD-BGR) with nano-watt (nW) power consumption. The PD-BGR consists of a current generator (CG) and differential voltage generator (DVG) $[29]$ . The CG is based on the bandgap reference (BGR) [\[7\]](#page-6-2) and generates a reference current and a voltage, and the DVG generates another voltage from the current. A differential voltage reference *V*<sub>REFD</sub> can be obtained by taking the voltage difference from these two voltages. Our proposed circuit can also produce a programmable differential voltage  $V_{\text{REFD}}$  by changing the multipliers of MOS-FETs in a differential pair and resistance with digital codes. The proposed PD-BGR can generate 25- to 200-mV programmable differential output voltages with a 25-mV step. In contrast to our previous work  $[29]$ , here, we describe circuit operation in more detail and conduct chip measurements fabricated with a  $0.18 - \mu m$  standard CMOS process technology.

This paper is organized as follows, Sect. 2 presents the proposed PD-BGR, Sect. 3 shows the results of simulations and measurements, and Sect. 4 concludes the paper.

# **2. Programmable Differential Bandgap Reference**

2.1 Characteristics of Subthreshold MOSFET and Bipolar Transistor

Before explaining our proposed PD-BGR architecture and

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<sup>†</sup>Division of Electrical, Electronic and Infocommunications Engineering, Graduate School of Engineering, Osaka University, Suita-shi, 565–0871 Japan.

a) E-mail: y.itotagawa@ssc.eei.eng.osaka-u.ac.jp



**Fig. 1** Block diagram of our proposed differential bandgap reference (©2023 IEEE [\[29\]](#page-7-1)).

its operation principle, we first briefly summarize the characteristics of the subthreshold current  $I_D$  of a MOSFET and base-emitter voltage *V*<sub>BE</sub> of a bipolar transistor as follows.

The subthreshold current  $I_D$  when the drain-source voltage  $V_{DS}$  exceeds 0.1 V is expressed as

$$
I_{\rm D} = K I_0 \exp\left(\frac{V_{\rm GS} - V_{\rm TH}}{\eta V_{\rm T}}\right),\tag{1}
$$

where *K* is the transistor aspect ratio,  $I_0 = \mu C_{OX} V_T^2(\eta - 1)$ is a process-dependent parameter,  $\mu$  is the carrier mobility,  $C_{OX}$  is the gate-oxide capacitance,  $V_T$  is the thermal voltage  $(V_T = k_B T/q)$ ,  $\eta$  is the subthreshold swing parameter,  $k_B$  is the Boltzmann constant, *T* is the absolute temperature, *q* is the elementary charge,  $V_{\text{GS}}$  is the gate-source voltage, and  $V_{TH}$  is the transistor threshold voltage  $[26]$ .

Regarding the bipolar transistor, in standard CMOS technology, the transistor generates a  $V_{BE}$  when it accepts a bias current  $I_{\text{B}}$ . The  $V_{\text{BE}}$  is expressed as

$$
V_{\rm BE} = V_{\rm T} \ln \left( \frac{I_{\rm S} + I_{\rm B}}{I_{\rm S}} \right) \approx V_{\rm T} \ln \left( \frac{I_{\rm B}}{I_{\rm S}} \right),\tag{2}
$$

where  $I<sub>S</sub>$  is the saturation current of a bipolar transistor [\[26\].](#page-7-2) For the first order approximation,  $V_{BE}$  decreases linearly with the temperature when we use a small temperature dependent bias current *I*BIAS. Thus, Eq. (2) can be simplified as

$$
V_{\rm BE} = V_{\rm BGR} - \gamma T,\tag{3}
$$

where *V*<sub>BGR</sub> is the bandgap voltage of silicon (i.e., ~1.2 V) and  $\gamma$  is the temperature coefficient of  $V_{\text{BE}}$ . In actual design, there will be higher order nonlinearities in the  $V_{BE}$ , but we consider the nonlinearities to be small compared with the first order temperature characteristics.

#### 2.2 Architecture and Operation Principle

Figure 1 shows a block diagram of our proposed PD-BGR consisting of a current generator (CG) and differential voltage generator (DVG). The CG generates a reference current *I*REF and voltage *V*<sub>OUT1</sub>. The DVG accepts the *I*<sub>REF</sub> and *V*<sub>OUT1</sub>, and generates *V*<sub>OUT2</sub>. A differential voltage reference *V*<sub>REFD</sub> can be obtained by taking the voltage difference



Fig. 2 Schematic of our proposed PD-BGR (©2023 IEEE [\[29\]](#page-7-1)).

between  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$ , or

$$
V_{\text{REFD}} = V_{\text{OUT2}} - V_{\text{OUT1}}.\tag{4}
$$

Figure 2 shows a schematic of our proposed PD-BGR. To achieve low-power and robust operation, a bandgap reference circuit proposed by *Banba et al.* is used as the CG [\[7\]](#page-6-2) (start-up circuit is not shown). The area ratio of bipolar transistors  $Q_1$  and  $Q_2$  and resistors  $R_1$ ,  $R_{1A}$ , and  $R_{1B}$  are set to 1 : *M* and  $R_1 = R_{1A} + R_{1B}$ , respectively, as shown in Fig. 2. The current  $I_{REF}$  flowing in the CG and the output voltage  $V<sub>OUT1</sub>$  are given by

$$
I_{\text{REF}} = \frac{V_{\text{BE1}}}{R_1} + \frac{V_{\text{BE1}} - V_{\text{BE2}}}{R_2},\tag{5}
$$

$$
V_{\text{OUT1}} = \frac{R_{1\text{B}}}{R_{1\text{A}} + R_{1\text{B}}} V_{\text{BE1}}.
$$
 (6)

By substituting Eqs.  $(2)$  and  $(3)$  into Eq.  $(5)$ ,  $I_{REF}$  is expressed as

$$
I_{\text{REF}} = \frac{V_{\text{BGR}}}{R_1} - \frac{\gamma T}{R_1} + \frac{V_{\text{T}} \ln(M)}{R_2}.
$$
 (7)

As shown in Eq.  $(7)$ , the temperature dependence of  $I_{REF}$  can be made small because those of the second and third terms are negative and positive, respectively [\[7\]](#page-6-2).

The DVG accepts the  $I_{REF}$  and  $V_{OUT1}$  as shown on the right in Fig. 2. The DVG consists of a differential pair circuit M1−M2, nMOS current mirror circuit, and resistor *R*3. The multipliers of transistors  $M_1$  and  $M_2$  are set to  $K_1$  and  $K_2$ , respectively. The current gain of the nMOS current mirror is set to  $1:1$ , and thus, currents flowing in transistors  $M_1$  and  $M_2$  become  $I_{REF}/2$ . Under this condition, the differential output voltage *V*<sub>REFD</sub> can be expressed as

$$
V_{\text{REFD}} = V_{\text{OUT2}} - V_{\text{OUT1}} = V_{\text{GS1}} - V_{\text{GS2}} + R_3 \frac{I_{\text{REF}}}{2},
$$
 (8)

where  $V_{GS1}$  and  $V_{GS2}$  are the gate-source voltages of  $M_1$  and M<sub>2</sub>, respectively. With Eqs. (1) and (7), the *V*<sub>REFD</sub> can be rewritten as



**Fig. 3** Schematic of programmable DVG: (a) programmable DVG core, (b)  $M_1$  (*l*-bit), (c)  $M_2$  (*m*-bit), and (d)  $R_3$  (*n*-bit) (©2023 IEEE [\[29\]\)](#page-7-1).

$$
V_{\text{REFD}} = V_{\text{TH1}} + \eta V_{\text{T}} \ln \left( \frac{I_{\text{REF}}/2}{K_1 I_0} \right) - V_{\text{TH2}} - \eta V_{\text{T}} \ln \left( \frac{I_{\text{REF}}/2}{K_2 I_0} \right)
$$
  
+ 
$$
\frac{R_3}{2} \left( \frac{V_{\text{BGR}}}{R_1} - \frac{\gamma T}{R_1} + \frac{V_{\text{T}} \ln(M)}{R_2} \right)
$$
  
= 
$$
\frac{R_3}{2R_1} V_{\text{BGR}} + \Delta V_{\text{TH}} - \frac{\gamma R_3}{2R_1} T
$$
  
+ 
$$
\left\{ \eta \ln \left( \frac{K_2}{K_1} \right) + \frac{R_3}{2R_2} \ln(M) \right\} \frac{k_{\text{B}}}{q} T,
$$
 (9)

where  $\Delta V_{\text{TH}}$  is the threshold voltage difference between M<sub>1</sub> and  $M_2$  in the differential pair and can be ignored when we use large-size MOSFETs and careful design techniques such as a common centroid layout  $[27]$ . Thus, Eq. (9) can be simplified to

$$
V_{\text{REFD}} = \frac{R_3}{2R_1} V_{\text{BGR}} - \frac{\gamma R_3}{2R_1} T + \left\{ \eta \ln \left( \frac{K_2}{K_1} \right) + \frac{R_3}{2R_2} \ln(M) \right\} \frac{k_B}{q} T.
$$
 (10)

From Eq. (10), a zero temperature coefficient of  $V_{\text{REFD}}$  can be obtained by designing the aspect ratios and resistors, or

$$
\frac{dV_{\text{REFD}}}{dT} = -\frac{\gamma R_3}{2R_1} + \left\{\eta \ln\left(\frac{K_2}{K_1}\right) + \frac{R_3}{2R_2} \ln(M)\right\} \frac{k_{\text{B}}}{q} = 0.
$$
\n(11)

Therefore, with the condition where Eq. (11) is satisfied, we obtain temperature compensated *V*<sub>REFD</sub> as

$$
V_{\text{REFD}} = \frac{R_3}{2R_1} V_{\text{BGR}}.\tag{12}
$$

## 2.3 Programmable DVG

As shown in Eqs. (11) and (12), we can obtain programmable

 $V_{REFD}$  by changing the ratio of  $R_1$  and  $R_3$  with a combination of  $R_2$ ,  $R_3$ ,  $K_1$ ,  $K_2$ , and  $M$ . In this work, we design the reference current  $I_{REF}$  to be constant (i.e.,  $R_1$ ,  $R_2$ , and  $M$  are set constant) and then control  $V_{\text{REFD}}$  by changing  $K_1, K_2$ , and  $R_3$  in the DVG.

Figure 3 (a) shows a schematic of a programmable DVG core circuit. The multipliers of  $M_1$  and  $M_2$  and the resistance of  $R_3$  are controlled by digital control signals of  $s_1[l - 1 : 0]$ , *s*2[*m* − 1 : 0], and *s*3[*n* − 1 : 0]. Figures 3 (b), 3 (c), and 3 (d) are detailed schematics of  $M_1$ ,  $M_2$ , and  $R_3$ . For  $M_1$  and M2, the same size transistors are connected or disconnected in parallel using switches and *l*- and *m*-bit control signals. With that, we can change the multipliers of  $M_1$  and  $M_2$ . For *R*3, *R*<sup>3</sup> is divided into *n*-th segment resistors, and the appropriate resistance is chosen using switches and *n*-bit control signals.

#### **3. Results**

## 3.1 Simulation Results

The performance of the proposed PD-BGR was evaluated by SPICE with a set of  $0.18$ - $\mu$ m standard CMOS process parameters. In this work, the resistors  $R_1$ ,  $R_2$ ,  $R_{1A}$ ,  $R_{1B}$ , and *M* were set to 59.6, 7.05, 32.8, 26.8 MΩ, and 8, respectively. The number of digital control bits was set to  $l = 2$ ,  $m = 8$ , and  $n = 8$ . Table 1 lists the design parameters  $K_1$ ,  $K_2$ , and  $R_3$  for the PD-BGR, where  $K_1$  and  $K_2$  are the multipliers of  $M_1$  and  $M_2$ .

Figure 4 shows the simulated  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$  as a function of temperature in the range of  $-20$  to  $100\degree C$ , when *V*REFD was set to 100 mV. The voltages decreased as the temperature increased. However, the  $V_{\text{REFD}} = V_{\text{OUT2}} - V_{\text{OUT1}}$ was kept almost constant at 100 mV.

Figure 5 shows the simulated *V*<sub>REFD</sub>s in the same temperature range. The *V*<sub>REFD</sub>s were set to from 25 to 200

**Table 1** Design parameters for PD-BGR.

$V_{REFD}$ (mV)	$K_1$	$K_2$	$R_3(M\Omega)$
25	64	78	2.3
50	32	45	4.8
75	64	102	7.3
100	32	59	9.7
125	32	69	12.3
150	64	150	14.9
175	32	89	17.3
200	32.	102	19.8



**Fig. 4** Simulated  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$  when  $V_{\text{REFD}}$  was set to 100 mV (©2023 IEEE [\[29\]](#page-7-1)).



**Fig. 5** Simulated programmable  $V_{REFD}$ .  $V_{REFD}$  was set to  $25 - 200$  mV with 25-mV step (©2023 IEEE [\[29\]\)](#page-7-1).

mV with a 25-mV step. Almost constant *V*<sub>REFD</sub>s were obtained. Figure 6 shows the temperature inaccuracy, derived from Fig. 5. Our PD-BGR achieved high accuracy, within a  $\pm 0.7\%$  inaccuracy.

We also performed a Monte Carlo simulation assuming die-to-die (D2D) global variations and within-die (WID) random mismatch variations in all MOSFETs and resistors[\[27\],](#page-7-3) [\[28\]](#page-7-4). The results for 1,000 runs, when the *V*<sub>REFD</sub> was set to 100 mV, are depicted in Fig. 7. The average value  $\mu$  and standard deviation  $\sigma$  of  $V_{\text{REFD}}$ , in the temperature range from  $-20$  to  $100\degree$ C were 100 and 0.87 mV, respectively. The coefficient of variation (CV=  $\sigma/\mu$ ) was 0.87%. Table 2 summarizes the characteristics of the simulated temperature coefficient (TC) and Monte Carlo simulation results of our proposed PD-BGR. In the simulation, we confirmed a highly



Fig. 6 Temperature inaccuracy of V<sub>REFD</sub> (©2023 IEEE [\[29\]\)](#page-7-1).



**Fig. 7** Distribution of  $V_{REFD}$  when  $V_{REFD}$  was set to 100 mV, as obtained from Monte Carlo simulation of 1,000 runs (©2023 IEEE [\[29\]](#page-7-1)).

**Table 2** Simulated TC and Monte Carlo simulation results.

$V_{REFD}$ (mV)	TC (ppm/°C)	$\mu$ (mV)	$\sigma$ (mV)	$\sigma/\mu(\%)$
25	100	25.0	0.29	1.10
50	28.1	50.0	0.44	0.88
75	11.9	75.0	0.63	0.83
100	15.8	100	0.87	0.87
125	24.4	125	1.06	0.85
150	44.0	150	1.28	0.86
175	35.6	175	1.48	0.85
200	40.5	200	1.75	0.88

stable PD-BGR, thanks to the reference circuit based on the bandgap voltage reference.

We consider the stability of the PD-BGR. As shown in Eq. (11), the variation of the TC will mainly come from the second term, or the characteristics of the DVG, because the first and third terms are basically stable and determined by the BGR-based CG. To investigate the effect of the process variation on the TC, we performed the Monte Carlo simulation again. Figure 8 shows the simulated average TC with different sizes of unit transistor in the DVG. We set the channel width  $(W)$  ( $\mu$ m) and length  $(L)$  ( $\mu$ m) of the unit transistor of M1 and M2 as  $W/L = 1/1, 3/3,$  and 5/5, respectively. The simulated average TC decreased as the unit transistor size increased. The TC can be made small,  $15.8$  ppm/ $°C$ , when we used the unit transistor size of  $W/L = 5/5$ .



**Fig. 8** Simulated average TC with different sizes of unit transistor.



**Fig. 9** Chip micrograph.



**Fig. 10** Measured  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$  when  $V_{\text{REFD}}$  was set to 100 mV.

## 3.2 Measurement Results

The proposed PD-BGR was fabricated with a set of  $0.18 - \mu m$ CMOS process technology. Figure 9 shows the chip micrograph. The total area of our proposed PD-BGR including the digital backend is  $0.438$  mm<sup>2</sup>.

Figure 10 shows the measured  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$  in the temperature range of  $-20$  to 100 $\degree$ C, when the *V*<sub>REFD</sub> was set to 100 mV. We also plotted the simulation results with gray color. The measured output voltages were almost the same as the simulation results, even though the errors from the simulation results increased as the temperature increased. However, the  $V_{\text{REFD}} = V_{\text{OUT2}} - V_{\text{OUT1}}$  was kept almost con-



Fig. 11 Measured programmable V<sub>REFD</sub> as a function of temperature.  $V_{REFD}$  was set to  $25 - 200$  mV with  $25 - W$  step.



Fig. 12 Measured V<sub>REFD</sub> inaccuracy as a function of temperature when  $V_{\text{REFD}}$  was set to 100 mV.

stant at 100 mV. The temperature errors in  $V_{\text{OUT1}}$  and  $V_{\text{OUT2}}$ were canceled by the voltage subtraction.

Figure 11 shows the measured *V*<sub>REFD</sub> for 5 samples in the same temperature range. As in the simulation, the  $V_{\text{REFD}}$ s were set to from 25 to 200 mV with a 25-mV step. We obtained almost the same voltages as the simulation results. Figure 12 shows the temperature inaccuracy, when  $V_{\text{REFD}}$ was set to 100 mV. The inaccuracy was larger than expected (see Fig. 6). This was because of the process variations. However, the absolute value of *V*<sub>REFD</sub> and its temperature dependence could be trimmed by the digital control techniques. As discussed in Sect. 2, the output reference voltage *V*REFD is given by Eq. (12) when Eq. (11) is satisfied. Therefore, the absolute value of  $V_{REFD}$  can be trimmed by  $R_1$  and *R*3, and its temperature characteristics can be compensated by *R*2, *K*1, *K*2, and *M*. If we develop binary-weighted control techniques for these parameters, it will be possible to trim the *V*REFD more accuracy. In this design, we designed the PD-BGR by changing three parameters,  $K_1$ ,  $K_2$ , and  $R_3$ , as shown in Table 1. In this case, one possible trimming method is the use of parameters not in use for the *V*<sub>REFD</sub> program. That is, trimming of the absolute value and temperature characteristics can be performed by  $R_1$  and  $R_2$ , respectively.

Figure 13 shows the measured temperature inaccuracy for all *V*<sub>REFD</sub>s. The measured temperature inaccuracy was kept within  $\pm 1\%$  except for  $V_{\text{REFD}} = 25$  mV in the temperature range from −20 to 80◦C, but became worse at high temperature above 80◦C. The reason for the degradation could be leakage current of MOSFETs. The temperature inaccuracy for  $V_{REFD} = 25$  mV was quite large even though the voltage spread of  $V_{\text{REFD}} = 25$  mV was comparable to others as shown in Table 3 (see MAX and MIN values in Table 3). One possible reason for this could be that the denominator of the temperature inaccuracy itself was low of  $V_{REFD} = 25$ mV.

Table 3 summarizes the measured *V*<sub>REFD</sub>s and TCs for 5 samples. The measured TCs had larger errors than the simulation results. The errors became large when the temperature was over 80<sup>°</sup>C, or when *V*<sub>REFD</sub> was set to 25 mV. When the temperature became over 80◦C, leakage current



**Fig. 13** Measured temperature inaccuracy of  $V_{REFD}$ s as a function of temperature

$V_{\rm REFD}$	Measured $V_{REFD}$ (mV)				$TC$ (ppm/ $\rm ^{\circ}C$ )		
(mV)	$\mu$	$\sigma$	MAX	МIN	μ	MAX	MIN
25	24.1	0.31	25.0	22.3	688	753	649
50	49.0	0.45	49.9	47.9	191	213	176
75	73.9	0.60	75.1	73.1	46.7	70.5	31.8
100	98.9	0.78	100	97.7	61.5	99.1	39.1
125	124	0.96	126	122	111	144	85.1
150	149	1.09	152	147	136	156	119
175	174	1.27	178	172	162	188	139
200	199	1.43	203	196	176	200	152

Table 3 Measured V<sub>REFD</sub>s and TCs among 5 samples.

from the body to the source of the MOSFET increased significantly and this caused the voltage errors. The effect of the leakage current could be large for the small  $V_{\text{REFD}}$  of 25 mV.

Figure 14 shows the measured *V*<sub>REFD</sub> as a function of power supply voltage  $V_{\text{DD}}$  in the range from 1.0 to 1.8 V when *V*<sub>REFD</sub> was set to 100 mV. Simulated *V*<sub>REFD</sub> was also plotted for comparison. Our proposed circuit can operate at higher than 1.2 V. The line regulation (LR) is given by  $LR = \Delta V_{REFD}(mV)/\Delta V_{DD}(V)$ , where  $\Delta V_{REFD}$  is the reference voltage change in the supply voltage change ∆*V*<sub>DD</sub>. The measured LR was 2.64 mV/V. We obtained the stable *V*<sub>REFD</sub> in the supply voltage range from 1.2 to 1.8 V.

Table 4 summarizes the characteristics of our PD-BGR in comparison with other CMOS differential BGRs in [\[14\]–](#page-6-8) [\[20\].](#page-6-13) Our proposed PD-BGR can generate 25- to 200-mV reference voltages with a 25-mV step. The measured inaccuracy was −4/+3 mV for 5 samples. The power consumption is the lowest, 88.4 nW. These significant achievements come from our proposed voltage reference architecture. As shown in Eq.  $(10)$ , the reference voltage  $V_{REFD}$  can be obtained by not only the conventional bandgap voltage reference circuit architecture, but also the proposed differential pair circuit consisting of MOSFETs operating in the subthreshold region. By using these, we can obtain compact and lowvoltage programmable output reference voltages with nanowatt power consumption.



**Fig. 14** Measured  $V_{REFD}$  as a function of power supply voltage  $V_{DD}$  when VREFD was set to 100 mV.

**Table 4** Performance summary and comparison.

Ref.	15	16	[17]	[14]	[18]	[19]	[20]	This work
Tech. $(\mu m)$	2.0	0.65	0.25	0.35	0.18	0.18	0.18	0.18
$V_{\rm DD}$		5	2.5	1.5	$0.9 - 1.8$	1.5, 2.2, 2.95	3.3	$1.2 - 1.8$
Temp. $(^{\circ}C)$	$0 - 100$	$\qquad \qquad$	$-50 - 150$	$-20 - 100$	$-20 - 115$	$-50 - 140$	$5 - 85$	$-20 - 100$
Programmable	N <sub>O</sub>	NO.	NO.	NO.	NO.	<b>YES</b>	<b>YES</b>	<b>YES</b>
$V_{\text{REFD}}$ (V)	2.48	2.01	1.01	0.01	0.315	1.22.7.2.00.7.2.80	1.25/2.05/2.88	$25.0 - 200$ mV
								$(25-mV$ step)
$\sigma$ (mV)	24	5.5	<b>NA</b>	<b>NA</b>	<b>NA</b>	$\pm 5, \pm 7, \pm 11$	0.8/2/2.5	(see Tab. 3)
Power	$6 \text{ mW}$	$2.2 \text{ mW}$	$0.98$ mW	4.6 $\mu$ W	$36 \mu W$	$63 \mu\text{A}$ †	50 $\mu$ A $\dagger$	88.4 nW††
TC (ppm/°C)	20.9	115	20	25	89.3	28/36/38	$<$ 13/38/38	(see Tabs. $2$ and $3$ )
$LR$ (mV/V) $\uparrow\uparrow\uparrow$	0.45	NA	NА	<b>NA</b>	2.9	<b>NA</b>	NA.	$2.64 +$
Meas./Sim.	Meas.	Meas.	Sim.	Sim.	Meas.	Sim.	Meas.	Meas.

†: Supply current, ††: Average of 5 samples, †††:LR : Line Regulation

## **4. Conclusion**

We presented a PD-BGR consisting of a CG and DVG. The CG generates a current and a voltage, while the DVG generates another voltage from the current. A differential reference voltage can be obtained by taking the voltage difference from the voltages. The PD-BGR can produce a programmable differential output voltage by changing the multipliers of MOSFETs in a differential pair and resistance with digital codes. Simulation results showed that our proposed PD-BGR can generate 25- to 200-mV reference voltages with a  $25-mV$  step within a  $\pm 0.7\%$  inaccuracy in a temperature range from -20 to 100◦C. A Monte Carlo simulation showed that our circuit was robust against process variation and that the CV of the  $V_{\text{REFD}}$  was less than 1.1%. Measurement results demonstrated that our prototype chips can generate stable programmable differential output voltages. The average power consumption was only 88.4 nW, with a voltage error of  $-4/+3$  mV with 5 samples.

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## **References**

- <span id="page-6-0"></span>[1] [J.A. Paradiso and T. Starner, "Energy scavenging for mobile and](http://dx.doi.org/10.1109/mprv.2005.9) [wireless electronics," IEEE Pervasive Comput., vol.4, no.1, pp.18–](http://dx.doi.org/10.1109/mprv.2005.9) [27, Jan.-March 2005. DOI: 10.1109/MPRV.2005.9](http://dx.doi.org/10.1109/mprv.2005.9)
- [2] [A.P. Chandrakasan, D.C. Daly, J. Kwong, and Y.K. Ramadass, "Next](http://dx.doi.org/10.1109/vlsic.2008.4585930) [generation micro-power systems," IEEE Symp. Very Large Scale](http://dx.doi.org/10.1109/vlsic.2008.4585930) [Integr. \(VLSI\) Circuits, pp.2–5, 2008. DOI: 10.1109/VLSIC.2008.](http://dx.doi.org/10.1109/vlsic.2008.4585930) [4585930](http://dx.doi.org/10.1109/vlsic.2008.4585930)
- [3] [R.J.M. Vullers, R.V. Schaijk, H.J. Visser, J. Penders, and C.V. Hoof,](http://dx.doi.org/10.1109/mssc.2010.936667) ["Energy harvesting for autonomous wireless sensor networks," IEEE](http://dx.doi.org/10.1109/mssc.2010.936667) [Solid-State Circuits Mag., vol.2, no.2, pp.29–38, Feb. 2010. DOI:](http://dx.doi.org/10.1109/mssc.2010.936667) [10.1109/MSSC.2010.936667](http://dx.doi.org/10.1109/mssc.2010.936667)
- [4] [D. Blaauw, D. Sylvester, P. Dutta, Y. Lee, I. Lee, S. Bang, Y. Kim, G.](http://dx.doi.org/10.1109/vlsit.2014.6894411) [Kim, P. Pannuto, Y.-S. Kuo, D. Yoon, W. Jung, Z. Foo, Y.-P. Chen,](http://dx.doi.org/10.1109/vlsit.2014.6894411) [S. Oh, S. Jeong, and M. Choi, "IoT design space challenges: Circuits](http://dx.doi.org/10.1109/vlsit.2014.6894411) [and systems," in Symp. VLSI Technol. Dig. Tech. Papers, pp.1–2,](http://dx.doi.org/10.1109/vlsit.2014.6894411) [2014. DOI: 10.1109/VLSIT.2014.6894411](http://dx.doi.org/10.1109/vlsit.2014.6894411)
- [5] [L.D. Xu, W. He, and S. Li, "Internet of things in industries: A](http://dx.doi.org/10.1109/tii.2014.2300753) [survey," IEEE Trans. Ind. Inform., vol.10, no.4, pp.2233–2243, Nov.](http://dx.doi.org/10.1109/tii.2014.2300753) [2014. DOI: 10.1109/TII.2014.2300753](http://dx.doi.org/10.1109/tii.2014.2300753)
- <span id="page-6-1"></span>[6] [S. Chen, H. Xu, D. Liu, B. Hu, and H. Wang, "A vision of IoT:](http://dx.doi.org/10.1109/jiot.2014.2337336) [Applications, challenges, and opportunities with China perspective,"](http://dx.doi.org/10.1109/jiot.2014.2337336) [IEEE Internet of Things J., vol.1, no.4, pp.349–359, Aug. 2014. DOI:](http://dx.doi.org/10.1109/jiot.2014.2337336) [10.1109/JIOT.2014.2337336](http://dx.doi.org/10.1109/jiot.2014.2337336)
- <span id="page-6-2"></span>[7] [H. Banba, H. Shiga, A. Umezawa, T. Miyaba, T. Tanzawa, S. Atsumi,](http://dx.doi.org/10.1109/4.760378) [and K. Sakui, "A CMOS bandgap reference circuit with sub-1-V](http://dx.doi.org/10.1109/4.760378) [operation," IEEE J. Solid-State Circuits, vol.34, no.5, pp.670–674,](http://dx.doi.org/10.1109/4.760378) [May 1999. DOI: 10.1109/4.760378](http://dx.doi.org/10.1109/4.760378)
- <span id="page-6-4"></span>[8] [Y. Osaki, T. Hirose, N. Kuroki, and M. Numa, "1.2-V supply,](http://dx.doi.org/10.1109/jssc.2013.2252523) [100-nW, 1.09-V bandgap and 0.7-V supply, 52.5-nW, 0.55-V sub](http://dx.doi.org/10.1109/jssc.2013.2252523)[bandgap reference circuits for nanowatt CMOS LSIs," IEEE J.](http://dx.doi.org/10.1109/jssc.2013.2252523)

[Solid-State Circuits, vol.48, no.6, pp.1530–1538, June 2013. DOI:](http://dx.doi.org/10.1109/jssc.2013.2252523) [10.1109/JSSC.2013.2252523](http://dx.doi.org/10.1109/jssc.2013.2252523)

- <span id="page-6-5"></span>[9] [G. De Vita and G. Iannaccone, "A Sub-1-V, 10 ppm/](http://dx.doi.org/10.1109/jssc.2007.899077)°C, nanopower [voltage reference generator," IEEE J. Solid-State Circuits, vol.42,](http://dx.doi.org/10.1109/jssc.2007.899077) [no.7, pp.1536–1542, July 2007. DOI: 10.1109/JSSC.2007.899077](http://dx.doi.org/10.1109/jssc.2007.899077)
- <span id="page-6-6"></span>[10] [K. Ueno, T. Hirose, T. Asai, and Y. Amemiya, "A 300 nW, 15](http://dx.doi.org/10.1109/jssc.2009.2021922) ppm/◦[C, 20 ppm/V CMOS voltage reference circuit consisting of](http://dx.doi.org/10.1109/jssc.2009.2021922) [subthreshold MOSFETs,"IEEE J. Solid-State Circuits, vol.44, no.7,](http://dx.doi.org/10.1109/jssc.2009.2021922) [pp.2047–2054, July 2009. DOI: 10.1109/JSSC.2009.2021922](http://dx.doi.org/10.1109/jssc.2009.2021922)
- <span id="page-6-7"></span>[11] [M. Seok, G. Kim, D. Blaauw, and D. Sylvester, "A portable 2](http://dx.doi.org/10.1109/jssc.2012.2206683) [transistor picowatt temperature-compensated voltage reference oper](http://dx.doi.org/10.1109/jssc.2012.2206683)[ating at 0.5 V," IEEE J. Solid-State Circuits, vol.47, no.10, pp.2534–](http://dx.doi.org/10.1109/jssc.2012.2206683) [2545, Oct. 2012. DOI: 10.1109/JSSC.2012.2206683](http://dx.doi.org/10.1109/jssc.2012.2206683)
- [12] [I. Lee, D. Sylvester, and D. Blaauw, "A subthreshold voltage reference](http://dx.doi.org/10.1109/jssc.2017.2654326) [with scalable output voltage for low-power IoT systems," IEEE J.](http://dx.doi.org/10.1109/jssc.2017.2654326) [Solid-State Circuits, vol.52, no.5, pp.1443–1449, May 2017. DOI:](http://dx.doi.org/10.1109/jssc.2017.2654326) [10.1109/JSSC.2017.2654326](http://dx.doi.org/10.1109/jssc.2017.2654326)
- <span id="page-6-3"></span>[13] [J.M. Lee, Y. Ji, S. Choi, Y.-C. Cho, S.-J. Jang, J.S. Choi, B. Kim,](http://dx.doi.org/10.1109/isscc.2015.7062945) [H.-J. Park, and J.-Y. Sim, "5.7 A 29nW bandgap reference circuit,"](http://dx.doi.org/10.1109/isscc.2015.7062945) [IEEE Int. Solid-State Circuits Conf. Dig. Tech. Papers, pp.1–3, 2015.](http://dx.doi.org/10.1109/isscc.2015.7062945) [DOI: 10.1109/ISSCC.2015.7062945](http://dx.doi.org/10.1109/isscc.2015.7062945)
- <span id="page-6-8"></span>[14] [K. Ueno, T. Hirose, T. Asai, and Y. Amemiya, "Floating millivolt](http://dx.doi.org/10.1109/iscas.2007.378776) [reference for PTAT current generation in subthreshold MOS LSIs,"](http://dx.doi.org/10.1109/iscas.2007.378776) [IEEE Int. Symp. Circuits and Systems, pp.3748–3751, 2007. DOI:](http://dx.doi.org/10.1109/iscas.2007.378776) [10.1109/ISCAS.2007.378776](http://dx.doi.org/10.1109/iscas.2007.378776)
- <span id="page-6-9"></span>[15] [M. Ferro, F. Salerno, and R. Castello, "A floating CMOS bandgap](http://dx.doi.org/10.1109/4.32027) [voltage reference for differential applications," IEEE J. Solid-State](http://dx.doi.org/10.1109/4.32027) [Circuits, vol.24, no.3, pp.690–697, June 1989. DOI: 10.1109/](http://dx.doi.org/10.1109/4.32027) [4.32027](http://dx.doi.org/10.1109/4.32027)
- [16] [T.L. Brooks and A.L. Westwick, "A low-power differential CMOS](http://dx.doi.org/10.1109/isscc.1994.344654) [bandgap reference," Proc. IEEE Int. Solid-State Circuits Conf.,](http://dx.doi.org/10.1109/isscc.1994.344654) [pp.248–249, 1994. DOI: 10.1109/ISSCC.1994.344654](http://dx.doi.org/10.1109/isscc.1994.344654)
- [17] [T. Ogawa, T. Ozeki, and K. Taniguchi, "Floating voltage reference](http://dx.doi.org/10.1002/ecjb.10117) [generator for A/D converters," Electronics and Communications in](http://dx.doi.org/10.1002/ecjb.10117) [Japan \(Part II: Electronics\), pp.20–23, 2003. DOI: 10.1002/ecjb.](http://dx.doi.org/10.1002/ecjb.10117) [10117](http://dx.doi.org/10.1002/ecjb.10117)
- [18] [E.K.F. Lee, "A low voltage CMOS differential/floating bandgap](http://dx.doi.org/10.1109/iscas.2015.7168677) [voltage reference circuit," IEEE Int. Symp. Circuits and Systems,](http://dx.doi.org/10.1109/iscas.2015.7168677) [pp.489–492, 2015. DOI: 10.1109/ISCAS.2015.7168677](http://dx.doi.org/10.1109/iscas.2015.7168677)
- <span id="page-6-12"></span>[19] [S. Del Cesta, P. Bruschi, A.N. Longhitano, R. Simmarano, and](http://dx.doi.org/10.1109/prime.2016.7519489) [M. Piotto, "A CMOS compact differential band-gap voltage refer](http://dx.doi.org/10.1109/prime.2016.7519489)[ence with programmable output," 2016 12th Conf. Ph.D. Research](http://dx.doi.org/10.1109/prime.2016.7519489) [in Microelectronics and Electronics \(PRIME\), pp.1–4, 2016. DOI:](http://dx.doi.org/10.1109/prime.2016.7519489) [10.1109/PRIME.2016.7519489](http://dx.doi.org/10.1109/prime.2016.7519489)
- <span id="page-6-13"></span>[20] [S. Del Cesta, A. Ria, R. Simmarano, M. Piotto, and P. Bruschi,](http://dx.doi.org/10.1109/esscirc.2017.8094513) ["A compact programmable differential voltage reference with un](http://dx.doi.org/10.1109/esscirc.2017.8094513)[buffered 4 mA output current capability and](http://dx.doi.org/10.1109/esscirc.2017.8094513)  $\pm 0.4$  % untrimmed [spread," IEEE Eur. Solid State Circuits Conf., pp.11–14, 2017. DOI:](http://dx.doi.org/10.1109/esscirc.2017.8094513) [10.1109/ESSCIRC.2017.8094513](http://dx.doi.org/10.1109/esscirc.2017.8094513)
- [21] [N.S. JovičIć and V.M. Rajović, "A floating linear voltage regulator](http://dx.doi.org/10.1109/access.2018.2832123) [for powering large-scale differential communication networks," IEEE](http://dx.doi.org/10.1109/access.2018.2832123) [Access, vol.6, pp.24669–24679, 2018. DOI: 10.1109/ACCESS.](http://dx.doi.org/10.1109/access.2018.2832123) [2018.2832123](http://dx.doi.org/10.1109/access.2018.2832123)
- <span id="page-6-10"></span>[22] [M. Caselli, E. Tiurin, S. Stanzione, and A. Boni, "An Ultra Low-](http://dx.doi.org/10.1109/tcsi.2022.3219587)[Power Programmable Voltage Reference for Power-Constrained Elec](http://dx.doi.org/10.1109/tcsi.2022.3219587)[tronic Systems," IEEE Trans Circuits and Systems I, Regular Papers,](http://dx.doi.org/10.1109/tcsi.2022.3219587) [vol.70, no.2, pp.618–630, Feb. 2023. DOI: 10.1109/TCSI.2022.](http://dx.doi.org/10.1109/tcsi.2022.3219587) [3219587](http://dx.doi.org/10.1109/tcsi.2022.3219587)
- <span id="page-6-11"></span>[23] T. Hirose, R. Yoshimura, T. Ido, T. Matsuoka, and K. Taniguchi, "Watch-dog circuit for quality guarantee with subthreshold MOSFET current," IEICE Trans. Electronic, vol.E87-C, no.11, pp.1910–1914, 2004.
- [24] [K. Ueno, T. Hirose, T. Asai, and Y. Amemiya, "A CMOS watch](http://dx.doi.org/10.1093/ietfec/e89-a.4.902)[dog sensor for certifying the quality of various perishables with a](http://dx.doi.org/10.1093/ietfec/e89-a.4.902) [wider activation energy," IEICE Trans. Fundam. Electronic Com](http://dx.doi.org/10.1093/ietfec/e89-a.4.902)[muncation Comput. Sci., vol.E89-A, no.4, pp.902–907, 2006. DOI:](http://dx.doi.org/10.1093/ietfec/e89-a.4.902) [10.1093/ietfec/e89-a.4.902](http://dx.doi.org/10.1093/ietfec/e89-a.4.902)
- <span id="page-7-0"></span>[25] [K. Ueno, T. Hirose, T. Asai, and Y. Amemiya, "CMOS smart sensor](http://dx.doi.org/10.1109/jssc.2007.891676) [for monitoring the quality of perishables," IEEE J. Solid-State Cir](http://dx.doi.org/10.1109/jssc.2007.891676)[cuits, vol.42, no.4, pp.798–803, April 2007. DOI: 10.1109/JSSC.](http://dx.doi.org/10.1109/jssc.2007.891676) [2007.891676](http://dx.doi.org/10.1109/jssc.2007.891676)
- <span id="page-7-2"></span>[26] [Y. Taur and T.H. Ning, "Fundamentals of Modern VLSI Devices,"](http://dx.doi.org/10.1017/9781108847087) [Cambridge, U.K.: Cambridge Univ. Press, 2002.](http://dx.doi.org/10.1017/9781108847087)
- <span id="page-7-3"></span>[27] [M.J.M. Pelgrom, A.C.J. Duinmaijer, and A.P.G. Welbers, "Matching](http://dx.doi.org/10.1109/jssc.1989.572629) [properties of MOS transistors," IEEE J. Solid-State Circuits, vol.24,](http://dx.doi.org/10.1109/jssc.1989.572629) [no.5, pp.1433–1439, Oct. 1989. DOI: 10.1109/JSSC.1989.572629](http://dx.doi.org/10.1109/jssc.1989.572629)
- <span id="page-7-4"></span>[28] [K.A. Bowman, S.G. Duvall, and J.D. Meindl, "Impact of die-to](http://dx.doi.org/10.1109/4.982424)[die and within-die parameter fluctuations on the maximum clock](http://dx.doi.org/10.1109/4.982424) [frequency distribution for gigascale integration," IEEE J. Solid-State](http://dx.doi.org/10.1109/4.982424) [Circuits, vol.37, no.2, pp.183–190, 2002. DOI: 10.1109/4.982424](http://dx.doi.org/10.1109/4.982424)
- <span id="page-7-1"></span>[29] [Y. Itotagawa, K. Atsumi, H. Sebe, D. Kanemoto, and T. Hirose, "A](http://dx.doi.org/10.1109/iscas46773.2023.10182130) [Programmable Differential Bandgap Reference for Ultra-Low-Power](http://dx.doi.org/10.1109/iscas46773.2023.10182130) [IoT Edge Node Devices," Proc. Int. Symp. Circuits and Systems](http://dx.doi.org/10.1109/iscas46773.2023.10182130) [\(ISCAS\), pp.1–5, 2023. DOI: 10.1109/ISCAS46773.2023.10182130](http://dx.doi.org/10.1109/iscas46773.2023.10182130)



**Daisuke Kanemoto** received the B.S. degree in Electronics and Information Science from Kyoto Institute of Technology, Kyoto, Japan, in 2004 and received the M.S. and Ph.D. degrees in Electronic Engineering from Osaka University, Osaka, Japan, in 2006, 2011. From November 2010, he was an assistant professor at the Department of Electronics, Graduate School of Information Science and Electrical Engineering, Kyushu University, Fukuoka, Japan. From April 2013, he was an assistant professor at the De-

partment of Research Interdisciplinary Graduate School of Medicine and Engineering, University of Yamanashi, Yamanashi, Japan. From May 2015, he was a visiting assistant professor at the Department of Electrical Engineering, Stanford University, Stanford, USA. From June 2019, he has been an associate professor at the Graduate School of Engineering Osaka University, Osaka, Japan. His research interests include analog circuits, mixed-signal integrated circuits and compressed sensing. He is an IEEE member.



Yoshinori Itotagawa recieved the B.S. degree in the Division of Electrical, Electronic and Infocommunications Engineering from Osaka University, Osaka, Japan, in 2022. He is currently working toward the M.S. degree at the same university. His current research interests are in ultra-low-power CMOS circuits design.



**Koma Atsumi** received the B.S. and M.S. degrees in the Division of Electrical, Electronic and Infocommunications Engineering from Osaka University, Osaka, Japan, in 2021 and 2023, respectively. In 2023, he joined Sony Semiconductor Solutions Corporation, Japan.



**Hikaru Sebe** recieved the B.S. and M.S. degrees in the Division of Electrical, Electronic and Infocommunications Engineering from Osaka University, Osaka, Japan, in 2019 and 2021, respectively. He is currently working toward the Ph.D. degree at the same university. His current research interests are in ultra-low-power and ultra-low-voltage CMOS circuits design.



**Tetsuya Hirose** received B.S., M.S., and Ph.D. degrees from Osaka University, Osaka, Japan, in 2000, 2002, and 2005, respectively. From 2004 to 2008, he was a Research Associate with the Department of Electrical Engineering, Hokkaido University, Sapporo, Japan. From 2008 to 2019, he was an Associate Professor with the Department of Electrical and Electronics Engineering, Kobe University, Kobe, Japan. Since 2019, he has been a Professor with the Division of Electrical, Electronic and Information Engi-

neering, Graduate School of Engineering, Osaka University, Suita, Japan. He has authored or co-authored over 200 journal and conference papers. His current research interests are extremely low-voltage and low-power analog/digital mixed-signal integrated circuit design and smart sensor systems. Dr. Hirose is a senior member of the Institute of Electrical and Electronics Engineers (IEEE), and a member of the Institute of Electronics, Information and Communication Engineers (IEICE), and the Japan Society of Applied Physics (JSAP). He was a recipient or co-recipient of the 10th Joint Research Award of the Semiconductor Technology Academic Research Center (STARC) in 2013, the Marubun Research Encouragement Awards in 2017, the IEICE Best Invited Paper Award in 2022, and more than 30 other international and domestic awards. He served as a Technical Program Committee Member of the International Conference on Solid-State Devices and Materials from 2010 to 2013, the Asian Solid-State Circuits Conference from 2011 to 2022, an Associate Editor for the IEICE Electronics Express from 2012 to 2015, the Chapter Secretary of the IEEE SSCS Kansai Chapter from 2015 to 2016, and a Guest Associate Editor for the special issues of IEICE Transactions on Fundamentals of Electronics, Communications and Computer Sciences and on Electronics from 2010 to 2023.